

# Sarkovskii's Theorem:

Given:  $3 < 5 < 7 < 9 < \dots$ ,  
 $2 \cdot 3 < 2 \cdot 5 < 2 \cdot 7 < \dots$   
 $2^2 \cdot 3 < 2^2 \cdot 5 < 2^2 \cdot 7 < \dots$   
 $\dots < 2^k < 2^3 < 2^2 < 2^1 < 2^0$

If a function has a point of period  $n$ , and  $m > n$  (in this ordering), then it has a point of period  $m$ .

Corollary: If  $f^2$  has a 3 cycle, it has cycles of all periods



Thm: If  $f(a)=b, f(b)=c, f(c)=d$ , and  $d \leq a < b < c$ , then  $\forall n, \exists x_0$  of period  $n$  (ie  $f^n(x_0) = x_0$  but  $f^{m < n}(x_0) \neq x_0$ )

